

Cambridge International AS Level

MATHEMATICS

Paper 2 Pure Mathematics 2

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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This document consists of 13 printed pages.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Mathematics Specific Marking Principles Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing. Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected. Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw). Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.

Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- DM or DB When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

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Abbreviations

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)

CWO Correct Working Only

ISW Ignore Subsequent Working

SOI Seen Or Implied

SC Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the

light of a particular circumstance)

WWW Without Wrong Working

AWRT Answer Which Rounds To

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Question	Answer	Marks	Guidance
1(a)	Use at least one relevant logarithm property correctly	M1	
	Obtain correct equation $\frac{2+x}{x} = 9$ or equivalent with no logarithms	A1	
	Obtain $x = \frac{1}{4}$	A1	
		3	
1(b)	Attempt value of y from $\tan y = 1 \div (their (a))$	M1	May be implied by an answer in degrees (76.0)
	Obtain 1.326	A1	AWRT; and no other answers in the range
		2	

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Question	Answer	Marks	Guidance		
2	Solve $5x = 5 - 2x$ to obtain $x = \frac{5}{7}$	B1	Allow AWRT 0.714		
	Attempt solution of linear equation where signs of $5x$ and $2x$ are the same	M1			
	Obtain $x = -\frac{5}{3}$	A1	Allow AWRT –1.67		
	Substitute their values correctly	M1	Substitution must be seen unless implied by a correct answer. Their values must come from consideration of $5 x = 5 - 2x$		
	Obtain $\left -6\right +\left 4\right $ and hence 10	A1			
	Alternative method for Question 2				
	State or imply non-modulus equation $25x^2 = (5-2x)^2$	B1			
	Attempt solution of 3-term quadratic equation	M1			
	Obtain $-\frac{5}{3}$ and $\frac{5}{7}$	A1	Allow AWRT 0.714 and AWRT -1.67		
	Substitute their values correctly	M1	Substitution must be seen unless implied by a correct answer. Their values must come from consideration of $5 x = 5 - 2x$		
	Obtain $\left -6\right +\left 4\right $ and hence 10	A1			
		5			

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Question	Answer	Marks	Guidance
3	Expand at least one of $\sin(2\theta + 30)$ and $\cos(2\theta + 60)$ correctly	B1	
	Attempt expansions and division by $\cos 2\theta$ to obtain equation in $\tan 2\theta$ only	*M1	
	Obtain $\tan 2\theta = \frac{4}{6\sqrt{3}}, \frac{2}{3\sqrt{3}}, \frac{2\sqrt{3}}{9}, 0.3849$	A1	OE
	Obtain $\theta = 10.5$	A1	AWRT, e.g. 10.525 A0 for 0.184 radians
	Use correct process to find second value of θ	DM1	$\frac{180^{\circ} + their2\theta}{2} \text{ or } 90^{\circ} + their\theta$ Allow if using radians correctly
	Obtain $\theta = 100.5$	A1 FT	AWRT; and no other answers within the range.
		6	

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Question	Answer	Marks	Guidance
4(a)	Integrate to obtain form ke^{2x+1}	M1	$k \neq 12$ If $k = 6$ need to see evidence of integration, e.g. use of square bracket notation
	Obtain correct $3e^{2x+1}$	A1	
	Apply limits correctly to obtain $3e^5 - 3e$	A1	or exact equivalent, indices must be simplified, but allow e^1 . A0 for addition of $+c$
		3	
4(b)	$State \tan^2 x = \sec^2 x - 1$	B1	
	Express $4\sin^2 2x$ in the form $k_1 + k_2 \cos 4x$	M1	Where $k_1 k_2 \neq 0$
	Obtain correct $2-2\cos 4x$	A1	
	Integrate to obtain form $k_3 \tan x + k_4 x + k_5 \sin 4x$	M1	Where $k_3 k_4 k_5 \neq 0$
	Obtain correct $\tan x + x - \frac{1}{2}\sin 4x$	A1	Condone absence of $\dots + c$
		5	

Question	Answer	Marks	Guidance
5(a)	Carry out division at least as far as $x^2 + kx$ or equivalent	M1	OE, e.g. comparing coefficients with coefficient of x^2 equal to 1 and attempt at a second coefficient.
	Obtain quotient $x^2 + 4x + 12$	A1	
	Confirm remainder is 7	A1	AG
		3	
5(b)	Include $(x-2)^2$ as a factor	M1	Must be a product of factors only SC B1 for $(x^2 - 4x + 4)(x^2 + 4x + 12)$
	Conclude $(x-2)^2(x^2+4x+12)$	A1	isw any attempt to factorise the quotient.
		2	
5(c)	Apply logarithms and use power law for $e^{-3y} = k$ where $k > 0$	M1	
	Obtain $y = -\frac{1}{3} \ln 2$, $\frac{1}{3} \ln \frac{1}{2}$	A1	Or exact equivalent Must be simplified e.g. not lne or $\frac{6}{3}$ ISW extra solutions but A0 if undefined solutions are included.
		2	

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Question	Answer	Marks	Guidance
6(a)	Obtain $x = 1$.	B1	Allow e^0 . Must come from correct work, e.g. $\ln x = 0$.
	Obtain $x = e^2$	B1	
	Differentiate to obtain at least one correct term	*M1	
	Obtain correct first derivative $\frac{2 \ln x}{x} - \frac{2}{x}$	A1	Allow $\frac{\ln x}{x} + \frac{\ln x}{x} - \frac{2}{x}$
			Allow $-\frac{2x}{x^2}$
	Substitute at least one of <i>their x</i> -values corresponding to $y = 0$ to find gradient	DM1	Allow unsimplified.
	Obtain gradient -2 [at A] and gradient $2e^{-2}$ at [B]	A1	Must be simplified.
		6	
6(b)	Equate first derivative to zero	M1	Their derivative must have at least 2 terms.
	Obtain $x = e$	A1	Allow e ¹
		2	

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Question	Answer	Marks	Guidance		
7(a)	Equate y to 3 and confirm $p = \frac{1}{2\sin 2p}$	B1	AG		
		1			
7(b)	Consider sign of $p - \frac{1}{2\sin 2p}$ or equivalent for 0.5 and 0.6	M1			
	Obtain -0.09 and 0.06 or equivalents and justify conclusion	A1	AG		
		2			
7(c)	Use iteration process correctly at least once	M1	Need to see 0.55494		
	Obtain final answer 0.557 only	A1	Allow recovery. Allow if iterations are to 4sf Allow if insufficient iterations seen.		
	Show sufficient iterations to 5 s.f. to justify answer or show sign change in interval [0.5565, 0.5575]	A1	If not starting at 0.55 then max marks M1A1A0		
		3			

Question	Answer	Marks	Guidance
7(d)	Obtain $\frac{\mathrm{d}x}{\mathrm{d}t} = 4 + 2\mathrm{e}^{2t}$	B1	
	Use product rule to find $\frac{dy}{dt}$	M1	Must be of the form $p \sin 2t + qt \cos 2t$
	Obtain $6\sin 2t + 12t\cos 2t$	A1	Allow unsimplified.
	Divide to obtain $\frac{dy}{dx}$ using their $\frac{dy}{dt}$ and $\frac{dx}{dt}$ correctly	DM1	Must have either B1 or previous M1.
	Obtain 0.826	A1	AWRT
		5	